

Coherent Sources

Two sources are said to be coherent if they have exactly same frequency and zero or constant phase difference.



Addition Of Coherent Wave

Resultant intensity

For bright fringes,

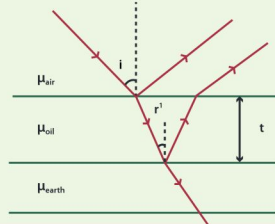
$$I_{\max} = (\sqrt{I_1} + \sqrt{I_2})^2 \text{ at } \Phi = 0, 2\pi, 4\pi, \dots$$

For dark fringes,

$$I_{\min} = (\sqrt{I_1} - \sqrt{I_2})^2 \text{ at } \Phi = \pi, 3\pi, 5\pi, \dots$$

$$I_1 = I_2 = I_0; I_R = 4I_0 \cos^2(\Phi/2)$$

Interference In Thin Film



For reflected light

$$\text{Maxima} \rightarrow 2\mu t \cos r = (2n+1)\frac{\lambda}{d}$$

$$\text{Minima} \rightarrow 2\mu t \cos r = n\lambda$$

For transmitted light

$$\text{Maxima} \rightarrow 2\mu t \cos r = n\lambda$$

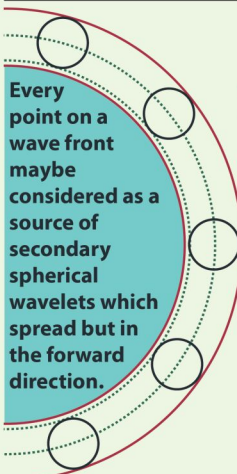
$$\text{Minima} \rightarrow 2\mu t \cos r = (2n+1)\frac{\lambda}{d}$$

Shift in fringe pattern

$$\Delta x = \frac{\beta}{\lambda}(\mu-1)t = \frac{D}{d}(\mu-1)t$$

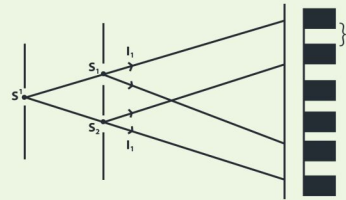
($\mu = \text{R.I. of the film}$)

Huygens Wave Theory



Every point on a wave front maybe considered as a source of secondary spherical wavelets which spread but in the forward direction.

Interference Of Light



The superposition of two coherent waves resulting in a pattern of dark and bright fringes of equal width.

$$\text{Position of bright fringe } x_n = \frac{n\lambda D}{d}$$

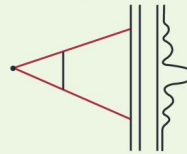
$$\text{Position of dark fringe } x_n' = \frac{(2n-1)\lambda D}{2d}$$

$$\text{Fringe width } \beta = \frac{\lambda D}{d}$$

Ratio of slit width with intensity

$$\frac{\omega_1}{\omega_2} = \frac{I_1}{I_2} = \frac{a_1^2}{a_2^2}$$

Diffraction



Single slit experiment

Angular position of n^{th} minima,

$$\theta_n = \frac{\lambda D}{d}$$

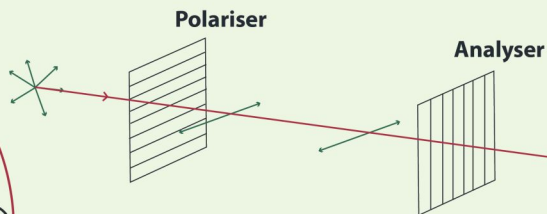
Angular position of n^{th} minima,

$$\theta_n = \frac{(2n+1)\lambda}{2d}$$

Width of central maximum,

$$\beta_0 = 2\beta = \frac{\lambda D}{d}$$

Polarisation Of Light



Malu's Law

The intensity of transmitted light passed through an analyser is

$$I = I_0 \cos^2 \theta$$

($\theta = \text{angle between transmission directions of polariser and analyser}$)

Polarisation By Reflection

Brewster's Law

The tangent of polarising angle of incidence at which reflected light becomes completely plane polarised is numerically equal to refractive index of the medium.

$$\mu = \tan i_p$$

&

$$i_p + r_p = 90^\circ \text{ (} i_p = \text{Brewster's angle)}$$

Doppler's Effect

Apparent frequency received during relative motion of source and observer

$$\gamma' = \gamma \left(1 - \frac{v}{c}\right); \text{ (red shift)}$$

$$\gamma' = \gamma \left(1 + \frac{v}{c}\right); \text{ (blue shift)}$$

Doppler shift

$$\Delta \gamma = \pm \frac{v}{c} \times \gamma$$

$$\Delta \lambda = \pm \frac{v}{c} \times \lambda \Rightarrow \lambda' - \lambda = \pm \frac{v}{c} \times \lambda$$